

# Package ‘geppe’

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**Type** Package

**Title** Generalised Exponential Poisson and Poisson Exponential Distributions

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**Depends** R (>= 4.0)

**Imports** Rfast2, stats

## Description

Maximum likelihood estimation, random values generation, density computation and other functions for the exponential-Poisson generalised exponential-Poisson and Poisson-exponential distributions. References include: Rodrigues G. C., Louzada F. and Ramos P. L. (2018). ``Poisson-exponential distribution: different methods of estimation''. Journal of Applied Statistics, 45(1): 128--144. <[doi:10.1080/02664763.2016.1268571](https://doi.org/10.1080/02664763.2016.1268571)>. Louzada F., Ramos, P. L. and Ferreira, H. P. (2020). ``Exponential-Poisson distribution: estimation and applications to rainfall and aircraft data with zero occurrence''. Communications in Statistics--Simulation and Computation, 49(4): 1024--1043. <[doi:10.1080/03610918.2018.1491988](https://doi.org/10.1080/03610918.2018.1491988)>. Barreto-Souza W. and Cribari-Neto F. (2009). ``A generalization of the exponential-Poisson distribution''. Statistics and Probability Letters, 79(24): 2493--2500. <[doi:10.1016/j.spl.2009.09.003](https://doi.org/10.1016/j.spl.2009.09.003)>.

**License** GPL (>= 2)

**NeedsCompilation** no

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geppe-package	<i>Generalised Exponential Poisson and Poisson Exponential Distributions</i>
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## Description

The package offers some functions (including MLE) for the exponential-Poisson (EP), the generalised EP (GEP) and the Poisson-exponential (PE) distributions.

## Details

Package:	geppe
Type:	Package
Version:	1.0
Date:	2024-06-23
License:	GPL-2

## Maintainers

Michail Tsagris <mtsagris@uoc.gr>.

## Author(s)

Michail Tsagris <mtsagris@uoc.gr> and Sofia Piperaki <sofiapip23@gmail.com>.

## References

- Barreto-Souza W. and Cribari-Neto F. (2009). A generalization of the exponential-Poisson distribution. *Statistics and Probability Letters*, 79(24): 2493–2500.
- Louzada F., Ramos P. L. and Ferreira H. P. (2020). Exponential-Poisson distribution: estimation and applications to rainfall and aircraft data with zero occurrence. *Communications in Statistics-Simulation and Computation*, 49(4): 1024–1043.
- Rodrigues G. C., Louzada F. and Ramos P. L. (2018). Poisson-exponential distribution: different methods of estimation. *Journal of Applied Statistics*, 45(1): 128–144.

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Density computation of the GEP, EP and PE distributions  
*Density computation of the GEP, EP and PE distributions*

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**Description**

Density computation of the GEP, EP and PE distributions.

**Usage**

```
depois(x, beta, lambda, logged = FALSE)
dgep(x, beta, alpha, lambda, logged = FALSE)
dpe(x, theta, lambda, logged = FALSE)
```

**Arguments**

<code>x</code>	A numerical vector with non-negative values.
<code>beta</code>	A strictly positive number, the scale parameter ( $\beta$ ).
<code>alpha</code>	A strictly positive number, the $\alpha$ parameter of the GEP distribution. If $a = 1$ , then one ends up with the EP distribution.
<code>theta</code>	A strictly positive number, the shape parameter ( $\theta$ ).
<code>lambda</code>	A strictly positive number, the shape parameter ( $\lambda$ ).
<code>logged</code>	Should the logarithm of the density values be computed? The default value is FALSE.

**Details**

The density values of the GEP, EP and PE distributions are computed. The density function of the EP is given by  $f(x) = \frac{\lambda\beta e^{-\lambda-\beta x+\lambda e^{-\beta x}}}{1 - e^{-\lambda}}$ .

The density function of the GEP is given by  $f(x) = \frac{\alpha\lambda\beta}{(1 - e^{-\lambda})^\alpha} \left(1 - e^{-\lambda+\lambda e^{-\beta x}}\right)^{\alpha-1} e^{-\lambda-\beta x+\lambda e^{-\beta x}}$ .

The density function of the PE is given by  $f(x) = \frac{\theta\lambda e^{-\lambda x-\theta e^{\lambda x}}}{1 - e^{-\theta}}$ .

**Value**

A vector with the (logged) density values.

**Author(s)**

Sofia Piperaki.

R implementation and documentation: Sofia Piperaki <sofiapip23@gmail.com> and Michail Tsagris <mtsagris@uoc.gr>.

## References

- Barreto-Souza W. and Cribari-Neto F. (2009). A generalization of the exponential-Poisson distribution. *Statistics and Probability Letters*, 79(24): 2493–2500.
- Louzada F., Ramos P. L. and Ferreira H. P. (2020). Exponential-Poisson distribution: estimation and applications to rainfall and aircraft data with zero occurrence. *Communications in Statistics-Simulation and Computation*, 49(4): 1024–1043.
- Rodrigues G. C., Louzada F. and Ramos P. L. (2018). Poisson-exponential distribution: different methods of estimation. *Journal of Applied Statistics*, 45(1): 128–144.

## See Also

[rgep](#), [pgep](#)

## Examples

```
x <- rgep(100, 1, 2, 3)
y <- dgep(x, 1, 2, 3, logged = TRUE)
sum(y)
```

Distribution function of the GEP, EP and PE distributions

*Distribution function of the GEP, EP and PE distributions*

## Description

Distribution function of the GEP, EP and PE distributions.

## Usage

```
pepois(x, beta, lambda)
pgep(x, beta, alpha, lambda)
ppe(x, theta, lambda)
```

## Arguments

- |                     |   |
|---------------------|---|
| <code>x</code>      | A numerical vector with non-negative values.  |
| <code>beta</code>   | A strictly positive number, the scale parameter ( $\beta$ ).  |
| <code>alpha</code>  | A strictly positive number, the $\alpha$ parameter of the GEP distribution. If $a = 1$ , then one ends up with the EP distribution. |
| <code>theta</code>  | A strictly positive number, the shape parameter ( $\theta$ ).   |
| <code>lambda</code> | A strictly positive number, the shape parameter ( $\lambda$ ).  |

## Details

The cumulative distribution values of the GEP, EP and PE distributions are computed. The probability function of the EP is given by  $f(x) = \frac{e^{\lambda e^{-\beta x}}}{1 - e^\lambda}$ .

The probability function of the GEP is given by  $f(x) = \left( \frac{1 - e^{-\lambda + \lambda e^{-\beta x}}}{1 - e^{-\lambda}} \right)^\alpha$ .

The probability function of the PE is given by  $f(x) = \frac{1 - e^{\theta - \theta e^{-\lambda x}}}{1 - e^{-\theta}}$ .

## Value

A vector with the cumulative distribution density values.

## Author(s)

Sofia Piperaki.

R implementation and documentation: Sofia Piperaki <sofiapip23@gmail.com> and Michail Tsagris <mtsagris@uoc.gr>.

## References

- Barreto-Souza W. and Cribari-Neto F. (2009). A generalization of the exponential-Poisson distribution. *Statistics and Probability Letters*, 79(24): 2493–2500.
- Louzada F., Ramos P. L. and Ferreira H. P. (2020). Exponential-Poisson distribution: estimation and applications to rainfall and aircraft data with zero occurrence. *Communications in Statistics-Simulation and Computation*, 49(4): 1024–1043.
- Rodrigues G. C., Louzada F. and Ramos P. L. (2018). Poisson-exponential distribution: different methods of estimation. *Journal of Applied Statistics*, 45(1): 128–144.

## See Also

[dgep](#), [qgep](#)

## Examples

```
x <- rgep(100, 1, 2, 3)
y <- pgep(x, 1, 2, 3)
```

### Maximum likelihood estimation of the GEP, EP and PE distributions

*Maximum likelihood estimation of the GEP, EP and PE distributions*

#### Description

Maximum likelihood estimation of the GEP, EP and PE distributions.

#### Usage

```
epois.mle(x)
gep.mle(x)
pe.mle(x)
```

#### Arguments

x	A numerical vector with non negative values.
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#### Details

Maximum likelihood estimation of the EP, GEP and PE distributions is performed.

#### Value

A list including:

param	A vector with the estimated values of $\alpha$ , $\beta$ , $\theta$ , $\lambda$ , depending on the distribution used.
loglik	The log-likelihood value of the distribution.

#### Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <[mtsagris@uoc.gr](mailto:mtsagris@uoc.gr)>.

#### References

- Barreto-Souza W. and Cribari-Neto F. (2009). A generalization of the exponential-Poisson distribution. *Statistics and Probability Letters*, 79(24): 2493–2500.
- Louzada F., Ramos P. L. and Ferreira H. P. (2020). Exponential-Poisson distribution: estimation and applications to rainfall and aircraft data with zero occurrence. *Communications in Statistics-Simulation and Computation*, 49(4): 1024–1043.
- Rodrigues G. C., Louzada F. and Ramos P. L. (2018). Poisson-exponential distribution: different methods of estimation. *Journal of Applied Statistics*, 45(1): 128–144.

#### See Also

[rgep](#)

## Examples

```
x <- rpois( 1000, 1, 3)
epois.mle(x)
```

Quantile function of the GEP, EP and PE distributions

*Quantile function of the GEP, EP and PE distributions*

## Description

Quantile function of the GEP, EP and PE distributions.

## Usage

```
qepois(p, beta, lambda)
qgep(p, beta, alpha, lambda)
qpe(p, theta, lambda)
```

## Arguments

p	A numerical vector with probability values.
beta	A strictly positive number, the scale parameter ( $\beta$ ).
alpha	A strictly positive number, the $\alpha$ parameter of the GEP distribution. If $a = 1$ , then one ends up with the EP distribution.
theta	A strictly positive number, the shape parameter ( $\theta$ ).
lambda	A strictly positive number, the shape parameter ( $\lambda$ ).

## Details

The quantiles of the GEP, EP and PE distributions are computed.

$$\text{The quantile function of the EP is given by } x_q = -\frac{\log [\lambda^{-1} \log (q(1 - e^\lambda) + e^\lambda)]}{\beta}.$$

$$\text{The quantile function of the GEP is given by } x_q = -\frac{\log [1 + \lambda^{-1} \log (1 - q^{1/\alpha}(1 - e^{-\lambda}))]}{\beta}.$$

$$\text{The quantile function of the PE is given by } x_q = \frac{\log (\theta) - \log [-\log (q - e^\theta (q - 1))]}{\lambda}.$$

## Value

A vector with the quantile values.

## Author(s)

Sofia Piperaki.

R implementation and documentation: Sofia Piperaki <sofiapip23@gmail.com> and Michail Tsagris <mtsagris@uoc.gr>.

## References

- Barreto-Souza W. and Cribari-Neto F. (2009). A generalization of the exponential-Poisson distribution. *Statistics and Probability Letters*, 79(24): 2493–2500.
- Louzada F., Ramos P. L. and Ferreira H. P. (2020). Exponential-Poisson distribution: estimation and applications to rainfall and aircraft data with zero occurrence. *Communications in Statistics-Simulation and Computation*, 49(4): 1024–1043.
- Rodrigues G. C., Louzada F. and Ramos P. L. (2018). Poisson-exponential distribution: different methods of estimation. *Journal of Applied Statistics*, 45(1): 128–144.

## See Also

[rgep](#), [pgep](#)

## Examples

```
y <- qgep(seq(0.1, 0.9, by = 0.1), 1, 2, 3)
```

Random values generation from the GEP, EP and PE distributions

*Random values generation from the GEP, EP and PE distributions*

## Description

Random values generation from the GEP, EP and PE distributions.

## Usage

```
repois(n, beta, lambda)
rgep(n, beta, alpha, lambda)
rpe(n, theta, lambda)
```

## Arguments

n	The sample size.
beta	A strictly positive number, the scale parameter ( $\beta$ ).
alpha	A strictly positive number, the $\alpha$ parameter of the GEP distribution. If $a = 1$ , then one ends up with the EP distribution.
theta	A strictly positive number, the shape parameter ( $\theta$ ).
lambda	A strictly positive number, the shape parameter ( $\lambda$ ).

## Details

In order to generate values from these distributions the inverse rejection sampling is used.

**Value**

A vector with generated values from the GEP, EP or the PE distribution.

**Author(s)**

Sofia Piperaki.

R implementation and documentation: Sofia Piperaki <sofiapip23@gmail.com> and Michail Tsagris <mtsagris@uoc.gr>.

**References**

- Barreto-Souza W. and Cribari-Neto F. (2009). A generalization of the exponential-Poisson distribution. *Statistics and Probability Letters*, 79(24): 2493–2500.
- Louzada F., Ramos P. L. and Ferreira H. P. (2020). Exponential-Poisson distribution: estimation and applications to rainfall and aircraft data with zero occurrence. *Communications in Statistics-Simulation and Computation*, 49(4): 1024–1043.
- Rodrigues G. C., Louzada F. and Ramos P. L. (2018). Poisson-exponential distribution: different methods of estimation. *Journal of Applied Statistics*, 45(1): 128–144.

**See Also**

[dgep](#)

**Examples**

```
x <- rgep(100, 1, 2, 3)
```

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